

# Exercises for Radiative Transfer in Astrophysics (SS2012)

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Exercise sheet 3

## Lambda Iteration

### 1. Multiple isotropic scattering in a 1-D plane-parallel atmosphere

Consider a semi-infinite ( $-\infty < z \leq 0$ ) 1-D vertical plane-parallel atmosphere with a constant extinction coefficient:  $\alpha = 1$  for  $z \leq 0$  (and  $\alpha = 0$  for  $z > 0$ ). The albedo  $\eta \equiv 1 - \epsilon$  is also constant. The value of the Planck function is taken to be  $B = 1$  for convenience. Let us use the *two-stream approximation* for the Lambda operator. At the top of the atmosphere we have an open boundary: Radiation can escape freely and no radiation enters the atmosphere. Let us put the bottom boundary at  $z = -10$  and put  $I_+ = 1$  as the bottom boundary condition. Use 100 gridpoints in  $z$ .

- (a) Write a computer program that solves this radiative transfer problem using Lambda Iteration.
- (b) Let us choose  $\epsilon = 0.5$ . Start with the mean intensity  $J(z) = 0$  as initial guess. Plot  $J(z)$  for consecutive iterations.
- (c) Now do the same for  $\epsilon = 10^{-1}$ . Notice that the convergence is slower.
- (d) Now try  $\epsilon = 10^{-3}$ . What do you see?

For all exercises, please always do the following:

- Make an electronic document (DOC or PDF) which includes your text concerning the exercises, as well as figures belonging to it.
- Upload your document *and your computer program* to the Moodle.